CONSTRAINTS ON THE COSMIC-RAY DENSITY GRADIENT BEYOND THE SOLAR CIRCLE FROM FERMI γ-RAY OBSERVATIONS OF THE THIRD GALACTIC QUADRANT


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ABSTRACT

We report an analysis of the interstellar γ-ray emission in the third Galactic quadrant measured by the Fermi Large Area Telescope. The window encompassing the Galactic plane from longitude 210° to 250° has kinematically well-defined segments of the Local and the Perseus arms, suitable to study the cosmic-ray (CR) densities across the outer Galaxy. We measure no large gradient with Galactocentric distance of the γ-ray emissivities per interstellar H atom over the regions sampled in this study. The gradient depends, however, on the optical depth correction applied to derive the H i column densities. No significant variations are found in the interstellar spectra in the outer Galaxy, indicating similar shapes of the CR spectrum up to the Perseus arm for particles with GeV to tens of GeV energies. The emissivity as a function of Galactocentric radius does not show a large enhancement in the spiral arms with respect to the interarm region. The measured emissivity gradient is flatter than expectations based on a CR propagation model using the radial distribution of supernova remnants and uniform diffusion properties. In this context, observations require a larger halo size and/or a flatter CR source distribution than usually assumed. The molecular mass calibrating ratio, X_{CO} = N(H_2)/W_{CO}, is found to be (2.08 ± 0.11) x 10^{20} cm^{-2}(K km s^{-1})^{-1} in the Local arm and is not significantly sensitive to the choice of H i spin temperature. No significant variations are found for clouds in the interarm region.

Key words: cosmic rays – gamma rays: ISM – ISM: general

Online-only material: color figures

1. INTRODUCTION

Knowledge of the distribution of cosmic-ray (CR) densities within our Galaxy is a key to understanding their origin and propagation. High-energy CRs interact with the gas in the interstellar medium (ISM) or the interstellar radiation field, and produce γ-rays via nucleon–nucleon interactions, electron Bremsstrahlung, and inverse Compton (IC) scattering. Since the ISM is transparent to these γ-rays, we can probe CRs in the local ISM, beyond direct measurements performed in the solar system, as well as in remote locations of the Galaxy. Although much effort has been made since the COS-B era (e.g., Strong et al. 1988; Strong & Mattox 1996; Bloemen et al. 1996), the results have been limited by the angular resolution, effective area, and energy coverage of the instruments. The advent of the Fermi Gamma-ray Space Telescope enables studying the spectral and spatial distribution of diffuse γ-rays and CRs with unprecedented sensitivity.

Here, we report an analysis of diffuse γ-ray emission observed in the third Galactic quadrant. The window with Galactic longitude 210° < l < 250° and latitude $-15^\circ < b < +20^\circ$ hosts kinematically well-defined segments of the Local and the Perseus spiral arms and is one of the best regions to study the CR density distribution across the outer Galaxy. The region has already been studied by Digel et al. (2001) using EGRET data. The improved sensitivity and angular resolution of the Fermi LAT (Large Area Telescope; Atwood et al. 2009) and recent developments in the study of the ISM allow us to examine the CR spectra and density distribution with better accuracy. We exclude from the analysis the region of the Monoceros R2 giant molecular cloud and the Southern Filament of the Orion–Monoceros complex (e.g., Wilson et al. 2005), in $l < 222^\circ$ and $b < -6^\circ$, because (1) star-forming activity and possible strong magnetic fields suggested by the filamentary structure (e.g., Morris et al. 1980; Maddalena et al. 1986) could indicate a special CR environment, and (2) an OB association in Monoceros R2 may hamper the determination of ISM densities from dust tracers (see Section 2.1.2 for details).

Study of the X_{CO} conversion factor which transforms the integrated intensity of the 2.6 mm line of carbon monoxide, W_{CO}, into the molecular hydrogen column density, N(H_2), is also possible since the region contains well-known molecular complexes. In the Local arm, we find the molecular clouds associated with Canis Major OB 1, NGC 2348, and NGC 2632 (Mel’nik & Efremov 1995; Kaltcheva & Hilditch 2000). At a few kpc from the solar system, in the interarm, lower-density region located between the Local and Perseus arms, we find Maddalena’s cloud (Maddalena & Thaddeus 1985), a giant molecular cloud remarkable for its lack of star formation, and the cloud associated with Canis Major OB 2 (Kaltcheva & Hilditch 2000).

This study complements the Fermi LAT study of the Cassiopeia and Cepheus region in the second quadrant reported by Abdo et al. (2010a). The paper is organized as follows. We describe the model preparation in Section 2 and the γ-ray observations, data selection, and the analysis procedure in Section 3. The results are presented in Section 4, where we also discuss the emissivity profile measured for the atomic gas and we compare it with predictions by a CR propagation model. A summary of the study is given in Section 5.

2. MODELING THE GAMMA-RAY EMISSION

2.1. Interstellar Gas

2.1.1. H i and CO

In order to derive the γ-ray emissivities associated with the different components of the ISM we need to determine the interstellar gas column densities separately for each region and gas phase. For atomic hydrogen we used the Leiden/Argentine/Bonn Galactic H i survey by Kalberla et al. (2005). In order to turn the H i line intensities into N(H i) column densities, a uniform spin temperature $T_S = 125$ K has often been adopted in previous studies. We will consider this option to directly compare our results with the former EGRET analysis of the same region (Digel et al. 2001) and other studies of the Galactic diffuse emission by the LAT (Abdo et al. 2009a, 2010a). Recent H i absorption studies (Dickey et al. 2009), however, point to larger average spin temperatures in the outer Galaxy, so we have tried different choices of $T_S$ to evaluate how the optical depth...
structures from the more massive Perseus arm component, provides more accurate estimates of the ISM column densities of Gaussian profiles. We believe that this separation procedure in the discussion.

in the Perseus arm, and will take this uncertainty into account i

Then, the spillover from one velocity interval to the next ones correction affects the results. We will find that the emissivity per H i atom and the inferred CR density is affected by up to ~50% in the Perseus arm, and will take this uncertainty into account in the discussion.

The integrated intensities of the 2.6 mm line of CO, $W_{\text{CO}}$, have been derived from the composite survey by Dame et al. (2001). The data have been filtered with the moment-masking technique in order to reduce the noise while keeping the resolution of the original data.

Figure 1 shows the velocity–longitude profile of H i emission in our region of interest (ROI). The preparation of maps accounting for the different Galactic structures present along the line of sight is similar to that described in detail in Abdo et al. (2010a) and based on a sequence of three steps:

1. preliminary separation within Galactocentric rings;
2. adjustment of the boundaries based on the velocity structures of the interstellar complexes;
3. correction for the spillover due to the velocity dispersion of the broad H i lines between adjacent regions.

Four regions were defined in Galactocentric distance, namely, the Local arm (Galactocentric radius $R \leq 10$ kpc), the interarm region ($R = 10–12.5$ kpc), the Perseus arm ($R = 12.5–16$ kpc), and the region beyond the Perseus arm (which hosts a faint segment of the outer arm; $R \geq 16$ kpc). The boundaries separating these regions under the assumption of a flat rotation curve (Clemens 1985) for the case of $R_0 = 8.5$ kpc and $\theta_0 = 220$ km s$^{-1}$ (where $R_0$ and $\theta_0$ are the Galactocentric radius and the orbital velocity of the local group of stars, respectively) are overlaid in Figure 1.

The preparation of the H i and CO gas maps started from these preliminary velocity boundaries, which were then adjusted for each line of sight to the closest minimum in the H i spectrum. Then, the spillover from one velocity interval to the next ones due to the velocity dispersion for the broad H i lines was corrected by fitting each H i spectrum with a combination of Gaussian profiles. We believe that this separation procedure provides more accurate estimates of the ISM column densities of each Galactic region than a simple slicing based on the rotation curve.

In particular, effort was put into separating the outer arm structures from the more massive Perseus arm component, especially at $l \gtrsim 235^\circ$ where the H i lines from the two regions merge into a single broad component. For directions where a minimum in the H i brightness temperature profile was not found near the $R = 16$ kpc velocity boundary, we integrated the profiles on both sides of the $R = 16$ kpc velocity boundary to estimate the Perseus and outer arm contributions. Then, we inserted a line in the Gaussian fitting at the outer-arm velocity extrapolated from the $l - v$ trend observed at $l \gtrsim 235^\circ$ to correct for the spillover due to the velocity dispersion. Given these difficulties we expect large systematic uncertainties in the outer-arm N(H i) column densities and the corresponding $\gamma$-ray emissivities will not be considered for the scientific interpretation. We note that the impact on the emissivities associated with the inner regions is small, ≤10% as described in Section 4.3.

The resulting maps are shown in Figures 2 and 3. They exhibit a low level of spatial degeneracy, and thus allow us to separate the $\gamma$-radiation arising from the interaction with CRs in each component.

2.1.2. Interstellar Reddening

It has been long debated whether the combination of H i and CO surveys traces total column densities of neutral interstellar matter. By comparing gas line surveys, the $\gamma$-ray observations by EGRET and dust thermal emission, Grenier et al. (2005) reported a considerable amount of neutral gas at the interface between the two H i and CO emitting phases, associated with cold dust but not properly traced by H i and CO observations. Their finding was then confirmed by LAT data for the Gould Belt in the second quadrant (Abdo et al. 2010a).

In order to complement the H i and CO maps, we have prepared a map derived from the $E(B - V)$ reddening map by Schlegel et al. (1998). The residual point sources at low latitudes were masked by setting to zero regions of $0.2$ radius centered on the positions of potential IRAS point sources46 if the $E(B - V)$ magnitude exceeded by $\gtrsim 20\%$ that in surrounding pixels. The masked regions were then restored through an inpainting technique (Elad et al. 2005). In the course of the work, various source masking techniques have been used with negligible impact on the H i and CO emissivity results.

The resulting map was fitted with a linear combination of the set of N(H i) and $W_{\text{CO}}$ maps described in Section 2.1.1. The operation was repeated for different choices of H i spin temperature. The fit was performed over the same region as for the $\gamma$-ray analysis, excluding a $3^\circ \times 3^\circ$ region centered around Canis Major OB 1 (Mel’nik & Efremov 1995) where the temperature correction applied by Schlegel et al. (1998) are less reliable with decreasing latitude, but the improvement we find in the $\gamma$-ray fit by adding the dust residual map supports the use of their map at low latitude.

The residual $E(B - V)_{\text{res}}$ map, after subtracting the linear combination of N(H i) and $W_{\text{CO}}$ maps, is shown in Figure 4 (left panel). The residuals typically range from $-0.5$ to $+0.5$ mag. Large regions of positive residuals are found along the Galactic plane, in association with molecular/atomic clouds. They are expected to trace gas not correctly traced by H i CO

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure1.png}
\caption{Longitude–velocity diagram of the average intensity of the 21 cm line (in unit of K) for $-15^\circ \leq b \leq 20^\circ$. Preliminary boundaries between the four Galactocentric annuli are also presented (see Section 2.1.1 for details). The lowest contour corresponds to 2 K and the contour interval is 3 K.}
\end{figure}

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45 The minima are unlikely to be due to self absorption, because the velocity-distance relation is single valued in the outer Galaxy.

surveys. A remarkable region of positive residuals is detected at intermediate latitudes around \( l = 245^\circ, b = +17^\circ \), in a region not covered by CO surveys. It corresponds to positive residuals also in \( \gamma \)-rays (Section 3.2) and may be due to a missing, but possibly CO-bright molecular cloud (already suggested by Dame et al. 2001 discussing the completeness of their survey, see Figure 8 of their paper). The negative residuals are generally small and may result from limitations in the gas column density derivation and/or dust spectral variations. The dust residual map compares well with the \( \gamma \)-ray residual map obtained when using only HI and CO to model the \( \gamma \)-ray emission (Figure 4, right panel). The correlation between the spatial distributions of the dust and \( \gamma \)-ray residuals is statistically confirmed in Section 3.2. Dust and \( \gamma \)-rays are consistent with the presence of missing gas in the positive residual clumps. The faint “glow” of negative residuals on both sides of the Galactic plane is driven by the nearby N(HI) maps and it remains even when using the smallest possible column densities derived in the optically thin case. It may suggest a small change in average spin temperature from the massive, compact clouds sampled in the plane to the more diffuse envelopes sampled off the plane, or it may be due to the presence of more missing gas in the plane than our templates can provide for in the fit. The dust-to-gas ratio as well as the \( \gamma \)-ray emissivity in the HI components would then be driven to higher values by the low latitude data and would slightly overpredict the data off the plane.

The interpretation of the \( E(B - V)_{\text{res}} \) map in this region of the sky is complicated by the lack of distance information for the dust emission. It is not possible to unambiguously assign the residuals to any of the regions under study. Since we aim at separating different regions along the lines of sight to investigate the CR density gradient in the outer Galaxy, using the HI and CO lines is essential. We have therefore used the \( E(B - V)_{\text{res}} \) map to correct for the total gas column densities. This approach is supported by the correlation we find between the dust and \( \gamma \)-ray data (Section 3.2). We also note that, since the dust contribution linearly correlated with the HI and CO maps has been removed in the \( E(B - V)_{\text{res}} \) map, this procedure allows us to extract the...
Figure 3. Maps of $W_{\rm CO}$ (in unit of K km s$^{-1}$) for the Local arm (top left), interarm (top right), and the Perseus arm (bottom left) regions. The small box in the bottom right corner indicates the area not considered in the analysis. The maps have been smoothed with a Gaussian of $\sigma = 0.25$ for display.

(A color version of this figure is available in the online journal.)

γ-ray emissivities that are actually correlated with the H I and CO components.

2.2. IC and Point Sources

To model γ-ray emission not related with interstellar gas, we referred to the GALPROP code (e.g., Strong & Moskalenko 1998; Strong et al. 2007) for γ-rays produced through IC scattering and to the first Fermi LAT catalog (1FGL) for point sources (Abdo et al. 2010b).

GALPROP47 (Strong & Moskalenko 1998; Strong et al. 2007) is a numerical code which solves the CR transport equation within the Galaxy and predicts the γ-ray emission produced via interactions of CRs with interstellar matter (nucleon–nucleon interaction and electron Bremsstrahlung) and low-energy photons (IC scattering). IC emission is calculated from the distribution of (propagated) electrons and the interstellar radiation fields developed by Porter et al. (2008). Here we adopt the IC model map produced in the GALPROP run 54_77Xvarh7S in which the CR electron spectrum is adjusted to agree with that measured by the LAT (Abdo et al. 2009b). This GALPROP model has been used in publications by the LAT collaboration such as Abdo et al. (2010c).

The 1FGL Catalog is based on the first 11 months of the science phase of the mission and contains 1451 sources detected at a significance $\gtrsim 4\sigma$ (the threshold is 25 in term of test statistic, TS48 ). For our analysis we considered 21 point sources in the ROI with TS larger than 50.

48 The test statistic is defined as

$$TS = 2(\ln L - \ln L_0),$$

where $L$ and $L_0$ is the maximum likelihood with and without including the source in the model, respectively. $L$ is conventionally calculated as

$$\ln(L) = \sum n_i \ln(\theta_i) - \sum \theta_i,$$

where $n_i$ and $\theta_i$ are the data and the model–predicted counts in each pixel denoted by the subscript $i$, respectively (see, e.g., Mattox et al. 1996). TS is expected to be distributed as a $\chi^2$ with $n - n_0$ degrees of freedom if the numbers of free parameters in the model are respectively $n$ and $n_0$ (4 for sources in the 1FGL Catalog).

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http://galprop.stanford.edu
2.3. Gamma-Ray Analysis Model

Following a well-established approach that dates back to the COS-B era (e.g., Lebrun et al. 1983), we modeled the \( \gamma \)-ray emission as a linear combination of maps tracing the column density of the ISM. This approach is based on a simple, but very plausible assumption: \( \gamma \)-rays are generated through interactions of CRs and the interstellar gas, and the ISM itself is transparent to \( \gamma \)-rays. Then, assuming that CR densities do not significantly vary over the scale of the interstellar complexes under study and that CRs penetrate clouds uniformly to their cores we can model the \( \gamma \)-ray intensities to first order as a linear combination of contributions from CR interactions with the different gas phases in the various regions along each line of sight.

We also added the IC model map by GALPROP and models for point sources taken from the 1FGL Catalog as described in Section 2.2. To represent the extragalactic diffuse emission and the residual instrumental background from misclassified CR interactions in the LAT detector, we also added an isotropic component. CR interactions with ionized gas are not explicitly included in the model. The mass column densities of ionized gas are poorly known, but their contribution is generally lower (\( \lesssim 10\% \)) than that of the neutral gas and its scale height is much larger (\( \sim 1 \text{ kpc} \)) compared with \( \sim 0.2 \text{ kpc} \); Cordes & Lazio 2002). We therefore expect the diffuse \( \gamma \)-ray emission originating from ionized gas to be largely accommodated in the fit by other components with large angular scales, such as the isotropic and IC ones, and to minimally impact the determination of the neutral gas emissivities.

Therefore, the \( \gamma \)-ray intensities \( I_\gamma(l,b) \) (\( \text{s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{MeV}^{-1} \)) can be modeled as

\[
I_\gamma(l,b) = \sum_{i=1}^{4} q_{N\text{H}_i} \cdot N(\text{H}_i)(l,b) + \sum_{i=1}^{3} q_{\text{CO}_i} \cdot W_{\text{CO}}(l,b) + q_{\text{EBV}} \cdot E(B-V)_{\text{hess}}(l,b) + I_{\text{IC}}(l,b) + I_{\text{iso}} + \sum_{j} I_{\text{PS}_j},
\]

(1)

where sum over \( i \) represents the combination of the Galactic regions, \( q_{N\text{H}_i} \) (\( \text{s}^{-1} \text{sr}^{-1} \text{MeV}^{-1} \)) and \( q_{\text{CO}_i} \) (\( \text{s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{MeV}^{-1} \)) are the emissivities per \( \text{H}_i \) atom and per \( \text{CO} \) unit, respectively. \( q_{\text{EBV}} \) (\( \text{s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{MeV}^{-1} \text{mag}^{-1} \)) is the emissivity per unit of the \( E(B-V)_{\text{hess}} \) map (for which independent normalizations are allowed between the positive and negative residuals; see Section 3.2). \( I_{\text{IC}} \) and \( I_{\text{iso}} \) are the IC model and isotropic background intensities (\( \text{s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{MeV}^{-1} \)), respectively, and \( I_{\text{PS}_j} \) represents the point-source contributions.

Compared to the EGRET study by Digel et al. (2001), we use two additional maps to better trace the ISM: the CO map in the Perseus arm and the \( E(B-V)_{\text{hess}} \) map.

3. DATA ANALYSIS

3.1. Observations and Data Selection

The LAT on board the Fermi Gamma-ray Space Telescope, launched on 2008 June 11, is a pair-tracking telescope, detecting photons from \( \sim 20 \text{ MeV} \) to more than \( 300 \text{ GeV} \). Details on the LAT instrument and pre-launch expectations of the performance can be found in Atwood et al. (2009), and the on-orbit calibration is described in Abdo et al. (2009c).

Routine science operations with the LAT started on 2008 August 4. We have accumulated events from 2008 August 4 to 2010 February 4 to study diffuse \( \gamma \)-rays in our ROI. During this time interval the LAT was operated in sky survey mode nearly all of the time, obtaining complete sky coverage every two orbits and relatively uniform exposures over time. We used the standard LAT analysis software, the Science Tools, and selected events satisfying the standard low-background event selection (the so-called Diffuse class; Atwood et al. 2009). We also required the reconstructed zenith angles of the arrival direction of photons to be less than \( 105^\circ \) and the center of the LAT field of view to be within \( 52^\circ \) from the zenith, in order to reduce the contamination of photons from the Earth limb. In addition, we excluded the period of time during which the LAT detected bright GRBs, i.e., GRB080916C (Abdo et al. 2009d).

Data and software are publicly available from the Fermi Science Support Center (http://fermi.gsfc.nasa.gov/ssc). For this analysis we used the P6 Diffuse selection and the Science Tools version v9r16p0.
using 13 logarithmically spaced energy bands from 100 MeV to 25.6 GeV, and a single band above 9.05 GeV. We then have compared the model and data in each energy band using a binned maximum-likelihood method with Poisson statistics in $0.25 \times 0.25$ bins; we thus did not assume an a priori spectral shape of each model component except for the IC emission. For the other components the convolution with the instrument response functions was performed assuming an $E^{-2}$ spectrum, and the integrated intensities were allowed to vary in each narrow energy bin. Changing the fixed spectral shape index over the range from $-1.5$ to $-3.0$ has a negligible effect on the obtained spectrum. In the highest energy band, we have set both the normalization and the spectral index free to accommodate the wider bin width. We used a post-launch response function, P6_V3_DIFFUSE, developed to account for the $\gamma$-ray detection inefficiencies due to pile-up and accidental coincidence in the LAT (Rando et al. 2009). We stopped at 25.6 GeV since the photon statistics do not allow us to reliably separate different gas components above this energy.

We started with point sources detected with high significance ($TS \geq 100$) in the 1FGL Catalog; we have 14 sources in our ROI for which the normalizations are set free. We also included eight sources lying just outside ($\leq 5^\circ$) of the region boundaries, with all the spectral parameters fixed to those in the 1FGL Catalog. As a starting point we used H $\alpha$ maps prepared for $T S = 125$ K. We added model components step by step as described below.

We first fitted the LAT data using Equation (1) without the IC contributions in the lowest energy band, with $E^{-2}$ spectral index for each energy band and confirmed that the fit improved significantly; the TS summed over 14 bands with separate fits in each band (i.e., 14 more free parameters) is 187.6. The $\gamma$-ray emission associated to the gas traced by CO in the Perseus arm is thus significantly detected by the LAT.

Next, we included the $E(B-V)_{\text{res}}$ map in the analysis. We allowed the independent normalizations between the positive and the negative part of the $E(B-V)_{\text{res}}$ map, and found that the normalizations differ with each other. We thus will use the independent normalizations hereafter. We chose this model to better represent the LAT data and constrain the CR distributions, and leave a detailed discussion about the use of dust as ISM tracer to a dedicated paper. The improvement of the fit is very significant: $TS = 1119.6$ for 28 more free parameters. The correlation between the $E(B-V)_{\text{res}}$ map and the $\gamma$-ray residual map obtained by the fit without the $E(B-V)_{\text{res}}$ map, shown in Figure 4, further supports the use of $E(B-V)_{\text{res}}$ map in our analysis.

We also tried a fit without the IC component to assess the systematics. The effects on the derived emissivities are typically 2%–3% and $\sim 5\%$ for $q_{H\alpha}$ and $q_{CO}$, respectively. They are much smaller than the statistical errors and systematic uncertainties (see below), although the inclusion of the IC map improves the fit to the LAT data. Therefore, the uncertainties on the IC model have no significant impact on our analysis due to its rather flat distribution across the ROI while the gas in the ISM is highly structured. On the other hand, lowering the threshold for point sources down to $TS = 50$ yields an about twice smaller emissivity for the WCO map in the Perseus arm. The emissivities of other components are unchanged within the statistical errors. This is plausible due to the very clumpy distribution of the clouds in the Perseus arm as seen by a terrestrial observer, see Figure 3, which makes it difficult to separate from that of some discrete sources. We thus use Equation (1) with point sources detected at $TS \geq 50$ in the 1FGL Catalog as our baseline model, but we do not consider the highly uncertain CO emissivities in the Perseus arm for the discussion.

We summarize the results in Tables 1 and 2 for $TS = 125$ K and 250 K, respectively, and the number of counts in each energy bin in Table 3. The differential emissivities are multiplied by $E^2$.
where $E$ is the center of each energy bin in logarithmic scale. They are given for each model component. We note that our isotropic term ($I_{iso}$) includes the contribution of the instrumental background and might partially account also for ionized gas (see Section 2.3), thus it is significantly larger than the extragalactic diffuse emission reported by Abdol et al. (2010d). To illustrate the fit quality, we give the data and model count maps and the residual map in Figure 5 (for $T_S = 125$ K), in which residuals (data minus model) are expressed in approximate standard deviation units (square root of model-predicted counts). Although some structures (clustering of positive or negative residuals) are observed, the map shows no excesses below $-4\sigma$ and above $6\sigma$. Over 99% of the pixels are within $\pm 3\sigma$. We thus conclude that our model reasonably reproduces the data.

Figure 6 presents the fitted spectra for each component. The emission from the H1 gas dominates the $\gamma$-ray flux. Although the emission from the gas in the CO-bright phase and that traced by $(B - V)_{res}$ is fainter than the IC and isotropic components, their characteristic spatial structures (see Figures 2 and 3) allow their spectra to be reliably constrained.

To examine the effect of the optical depth correction applied to derive the H1 maps, as anticipated above we tried several choices of a uniform $T_S$. We stress that the true $T_S$ is likely to vary within clouds, but we stick to this simple approximation exploring the following values: 100 K (which is a reasonable lower limit in the uniform approximation), $51^1 250$ K and $400$ K (which are the two values indicated by absorption measurements in the outer Galaxy by Dickey et al. 2009), $52^1$ and the optically thin approximation (which yields the lower limit allowed on the atomic column densities). The results on the maximum log-likelihood values are summarized in Table 4 together with the integrated H1 emissivities obtained above 100 MeV in each region. The evolution of $\ln(L)$ with $T_S$ is plotted in Figure 7. The H1 emissivity varies by $+15\%$ -- $-10\%$ for the Local arm, $+10\% / -0\%$ for the interarm region, and $+50\% / -25\%$ for the Perseus arm with respect to the $T_S = 125$ K case. We observe an increase of $\ln(L)$ with increasing spin temperature. Considering the fact that $T_S = 250$ K is a typical value in the second quadrant of the outer Galaxy according to a recent study by Dickey et al. (2009) and because $\ln(L)$ saturates at $T_S \geq 250$ K, we regard 250 K as a plausible estimate of the average $T_S$ in our ROI. Unfortunately, the estimates by Dickey et al. (2009) have a rather large uncertainty (about $\pm 50$ K) in each Galactocentric radius bin, and they do not cover the region in the third quadrant we are investigating (see Figure 5 of Dickey et al. 2009). In the following sections, we will concentrate on $T_S = 125$ K for comparison with previous $\gamma$-ray measurements and on $T_S = 250$ K which agrees well with H1 absorption and the LAT data.

4. RESULTS AND DISCUSSIONS

4.1. Emissivity Spectra of Atomic Gas

In Figures 8 and 9 (left panels), we report the emissivity spectra found per H atom in the Local arm, interarm, Perseus arm

51 A truncation at 95 K was applied for channels where the brightness temperature was larger.

52 Note that, however, the data used by Dickey et al. (2009) do not cover the third Galactic quadrant.
and outermost regions for $T_S = 125$ and 250 K, respectively. For comparison with the local interstellar spectrum (LIS) we also plot the model spectrum used in Abdo et al. (2009a) which agrees well with LAT data in a mid-to-high-latitude region ($22^\circ \leq |b| \leq 60^\circ$) of the third quadrant (assuming $T_S = 125$ K). We see that the spectral shape of the Local arm emissivity agrees well with the model for the LIS and does not depend on the choice of spin temperature. The integral emissivity of the Local arm is 10% lower than that reported by Abdo et al. (2009a) for the same spin temperature. This difference is not significant given the uncertainties in the kinematic separation of the gas components. The present result is also consistent with the measurement in the second quadrant (Abdo et al. 2010a). Together they show that the CR density along the Local arm is rather uniform within 1 kpc around the Sun, both in the second and third quadrants.

Figure 5. Data count map (top left), model count map (top right), and the residual (data minus model) map in units of standard deviations (bottom left, saturated between $-3\sigma$ and $+3\sigma$) above 100 MeV obtained by our analysis. Point sources with $TS \geq 50$ in the 1FGL included in the fit are shown by crosses in the model map. Data/model count maps are in $0.25^\circ \times 0.25^\circ$ pixels, and the residual map has been smoothed with a Gaussian of $\sigma = 0.5^\circ$.

Table 4

<table>
<thead>
<tr>
<th>$T_S$</th>
<th>$\ln(L)$</th>
<th>$q_{H\perp 1}(E \geq 100\text{MeV})$</th>
<th>$q_{H\perp 2}(E \geq 100\text{MeV})$</th>
<th>$q_{H\perp 3}(E \geq 100\text{MeV})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>100 K</td>
<td>114407.6</td>
<td>$1.32 \pm 0.04$</td>
<td>$1.27 \pm 0.05$</td>
<td>$0.86 \pm 0.06$</td>
</tr>
<tr>
<td>125 K</td>
<td>114480.1</td>
<td>$1.47 \pm 0.05$</td>
<td>$1.26 \pm 0.06$</td>
<td>$1.14 \pm 0.08$</td>
</tr>
<tr>
<td>250 K</td>
<td>114533.8</td>
<td>$1.62 \pm 0.04$</td>
<td>$1.35 \pm 0.05$</td>
<td>$1.53 \pm 0.06$</td>
</tr>
<tr>
<td>400 K</td>
<td>114544.5</td>
<td>$1.67 \pm 0.07$</td>
<td>$1.39 \pm 0.08$</td>
<td>$1.64 \pm 0.09$</td>
</tr>
<tr>
<td>Optimally thin</td>
<td>114552.8</td>
<td>$1.70 \pm 0.07$</td>
<td>$1.39 \pm 0.07$</td>
<td>$1.77 \pm 0.09$</td>
</tr>
</tbody>
</table>

Notes.

a Units: $q_{H\perp i}(10^{-26} \text{photons s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1})$.

b The subscripts refer to the regions defined to perform the analysis: (1) Local arm, (2) interarm region, (3) Perseus arm.
The comparison of the data with the model emissivity expected for the Local arm region based on locally measured CRs (Figures 8 and 9) indicates a better fit for higher $T_S$; $T_S = 125$ K gives emissivities 15%-20% lower than the model, whereas $T_S = 250$ K shows better agreement by about 10%. Although the theoretical emissivity has uncertainties due to imperfect knowledge of the CR spectrum (see Abdo et al. 2009a), the fact that a high $T_S$ value yields a better match both to the local absolute emissivity and to the spatial distribution of the diffuse emission (Figure 7) leads to a value conventionally used in $\gamma$-ray astrophysics (125 K). This is in accord with independent estimates of $T_S$ as discussed in Section 3.2.

We also observe that the emissivity spectra do not vary significantly with Galactocentric distances in the outer Galaxy. To examine the spectral shape more quantitatively, we present the emissivity ratios of the interarm and Perseus regions relative to the Local arm in the right panels of Figures 8 and 9. The spectral shape in the interarm region is found to be consistent with that in the Local arm; a fit to the data for $T_S = 125$ K with a constant ratio gives $\chi^2 = 7.3$ for 13 degrees of freedom. Although the fit is not fully acceptable for the Perseus arm ($\chi^2 = 24.3$), the large $\chi^2$ is driven solely by the last bin. We note a possible interplay between the Perseus arm and the adjacent outer-arm emissivities in the highest energy bins (see left panels of Figures 8 and 9). It can be due to a small but non-negligible spatial difference between the modeled templates and data and/or to the presence of unresolved point sources (generally harder than diffuse emission). Photon fluctuations from the structured gas components can also lead the fit to a slightly different solution in the spatial separation of the components. One would expect these possible systematic uncertainties to become important at high energy given the limited counts in the overall map. It is difficult to quantitatively test these effects without knowledge of the true model distributions, but we can note that the small deviations seen at 400–560 MeV and 1.6–2.2 GeV from a constant ratio are not confirmed by the general trend of the other points. They indicate that there are systematic uncertainties not fully accounted for by the statistical errors in the fit. We thus do not claim nor deny the spectral softening of the Perseus arm at high energy. A test using $T_S = 250$ K for the $N(H_\text{i})$ maps gives the same conclusion on the spectral shape. We thus conclude that the spectral shapes are consistent with the LIS in the 0.1–6 GeV energy band, independent of the assumed $T_S$. Considering that these $\gamma$-rays trace CR nuclei of energies from a few GeV to about 100 GeV (see, e.g., Figure 11 of Mori 1997), LAT data indicate that the energy distribution of the main...
component of Galactic CRs does not vary significantly in the outer Galaxy in the third quadrant. We note that Abdo et al. (2010a) reported a possible spectral hardening in the Perseus arm in the second quadrant. This might be due to the presence of the very active star-forming region of NGC 7538 and of CRs having not diffused far from their sources, or to contamination by hard unresolved point sources. In fact, Abdo et al. (2010a) did not rule out the possibility that their result is due to systematic effects.

4.2. Calibration of Molecular Masses

High-energy γ-rays are a powerful probe to determine the CO-to-H$_2$ calibration ratio, $X_{\text{CO}}$, if the CR flux is comparable in the different gas phases inside a cloud. Since the γ-ray emission from the molecular gas is primarily due to CR interactions with H$_2$, and since the molecular binding energy is negligible in processes leading to γ-ray production, the emissivity per H$_2$ molecule is expected to be twice the emissivity per H$_1$ atom. Then, under the hypothesis that the same CR flux penetrates the H$_1$ and CO-bright phases of an interstellar complex, we can calculate $X_{\text{CO}}$ as $q_{\text{CO}} = 2X_{\text{CO}} \cdot q_{\text{H}_1}$.

We show $q_{\text{CO}}$ as a function of $q_{\text{H}_1}$ for the Local arm and the interarm region in Figure 10. We do not consider the correlation in the Perseus arm, because $q_{\text{CO}}$ from this region is affected by large systematic uncertainties (see Section 3.2). Since the emissivity associated with the CO-bright gas is not well determined in the lowest energy range (see Tables 1 and 2) because of the poor angular resolution of the LAT, and the fit at very high energy is affected by larger uncertainties (Section 4.1), we have plotted only data in the 200 MeV–9.05 GeV range. The linear correlation supports the assumption that Galactic CRs penetrate molecular clouds uniformly to their cores. It also suggests that contamination from point sources and CR spectral variations within the clouds are small.

We have derived the maximum-likelihood estimates of the slope and intercept of the linear relation between $q_{\text{CO}}$ and $q_{\text{H}_1}$, taking into account that $q_{\text{CO}}$ and $q_{\text{H}_1}$ are both measured (not true) values with known uncertainties. The resulting intercepts are compatible with zero. The $X_{\text{CO}}$ values we have obtained for $T_s = 125$ K and $250$ K are shown in Figure 8 but for $T_s = 250$ K.

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densities from the optical depth correction can impact the $X_{\text{CO}}$ determination in two ways: first by changing the $q_{\text{HI}}$ emissivity and second by modifying the $N(\text{H}^1)$ contrast within the cloud, hence the $\text{H}^1$ and CO separation. The global impact is mild since we find $X_{\text{CO}} = (1.56 \pm 0.17) \times 10^{20} \text{cm}^{-2}(\text{K km s}^{-1})^{-1}$ in the interarm region for $T_S = 125$ K.

Abdo et al. (2010a) reported comparable values of $X_{\text{CO}}$ in the second quadrant for $T_S = 125$ K; they obtained $(1.59 \pm 0.17) \times 10^{20} \text{cm}^{-2}(\text{K km s}^{-1})^{-1}$ and $(1.9 \pm 0.2) \times 10^{20} \text{cm}^{-2}(\text{K km s}^{-1})^{-1}$ for the Local arm ($R \leq 10$ kpc) and the Perseus arm. Given the systematic uncertainty in $X_{\text{CO}}$, roughly of the order of $0.3 \times 10^{20} \text{cm}^{-2}(\text{K km s}^{-1})^{-1}$, due to $\text{H}^1$ optical depth correction, the results of both studies point to a rather uniform ratio over several kpc in the outer Galaxy. Yet, these values are twice larger than found in the Galactic disk. Here we do not include the results for the optically thin approximation which is equivalent to an infinitely high $T_S$ and gives similar emissivities to $T_S = 400$ K. The typical statistical errors associated with these measurements are illustrated in the right panel for the $T_S = 125$ K case. In the right panel, a shaded area shows the characteristic systematic error due to the LAT event selection efficiency, evaluated to be $\sim 10\%$ in the energy range under study.

In order to evaluate the impact of the delicate separation of the gas in the outermost region, we have compared two extreme cases. The first one adopts the kinematic $R = 16$ kpc boundary and applies no correction for velocity dispersion and the second assigns all the outer-arm gas to the Perseus arm. The emissivity in the Perseus arm differs by about 5% from the original one, and those in the Local arm and interarm regions hardly change. Therefore, these effects are significantly smaller than the uncertainties due to the optical depth correction of the H$^1$ data. We also note that the main effect of the LAT selection efficiency uncertainty is to rigidly shift the profile without any significant impact on the gradient.

We thus conclude that the most important source of uncertainty in the CR density gradient derivation is currently that in the $N(\text{H}^1)$ determination. This is mainly because the optical depth correction is larger for dense H$^1$ clouds in the Local and Perseus arms than for diffuse clouds in the interarm region. The loss in contrast between the dense (low-latitude) and more diffuse (mid-latitude) H$^1$ structures resulting from an increase in spin temperature affects the fit, particularly in the Perseus component which is more narrowly concentrated near the plane. When probing the CR densities as the “ratio” between the observed numbers of $\gamma$-rays to H atoms, at the precision provided by the LAT the uncertainties in the ISM densities are dominant.

### 4.3.1. Comparison with EGRET and the Arm/interarm Contrast

An interesting finding of the former EGRET analysis (Digel et al. 2001) was an enhancement of the $\gamma$-ray emissivity in the Perseus arm compared with the interarm region. This possibility is relevant for models of diffuse $\gamma$-ray emissions based on the assumption that CR and ISM densities are coupled (e.g., Hunter et al. 1997, and references therein).

The Local arm emissivity obtained by the EGRET study for $T_S = 125$ K is $(1.81 \pm 0.17) \times 10^{-26} \text{photons s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1}$, which is $\sim 25\%$ larger than our LAT result. However, the two

**Figure 11.** Left: emissivity gradient for several choices of $T_S$. Right: emissivity gradient obtained by the LAT compared with the EGRET results under the assumption of $T_S = 125$ K. The shaded area indicates the systematic uncertainty in the LAT selection efficiency of $\sim 10\%$. The EGRET points have been downscaled by 20% to account for the change in $H^1$ survey data between the two studies (see Section 4.3.1).
studies are based on different H\textsc{i} surveys which yield different total N(H\textsc{i}) column densities integrated along the lines of sight. The column density ratios between the surveys varies from 0.6 to 1.0 within the ROI, with an average value of \(\sim 0.8\). The difference is likely due to the improved correction for stray-radiation in the more recent survey, as discussed in Kalberla et al. (2005). The EGRET Local arm emissivity scaled by 0.8 is in good agreement with our result for the same spin temperature. If we do not include the \(E(B-V)_{\text{res}}\) map in the fitting, we obtain an emissivity of \((1.68 \pm 0.05) \times 10^{-26}\) photons \(\text{s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1}\) which is still consistent with the down-scaled EGRET result within \(\sim 15\%\). We thus conclude that our result is consistent with the previous study but is more reliable because of higher \(\gamma\)-ray statistics, finer resolution, and an improved H\textsc{i} gas survey.

We can therefore compare the present emissivity gradient (for consistency in the case \(T_S = 125\) K) with that reported by the EGRET study, as summarized in Figure 11 (right panel in which the EGRET results multiplied by 0.8 are also shown). Although we observe good agreement between the two studies in the Local and the Perseus arms, this is not true for the arm/interarm contrast. The difference could be due to the simple partitioning in cloud velocity used for the EGRET study. The H\textsc{i} mass obtained for clouds in the interarm region with the simple partitioning is 20\%–40\% larger (for \(T_S = 125\) K) than with our separation scheme, exaggerating the amount of gas in the interarm region, and thus lowering the emissivity by the same amount. Our emissivity profile is thus consistent with the previous study, but with improved precision (smaller statistical errors) and accuracy (more reliable region separation method and better estimation of the point source contributions). We thus do not confirm a marked drop in the interarm region.

Low spin temperatures yield a smooth decline in H\textsc{i} emissivity to \(R \approx 16\) kpc in the outer Galaxy, without showing a significant coupling with ISM column densities. The Perseus-to-interarm contrast is at most of the order of 15\%–20\% for high spin temperatures as shown in the left panel of Figure 11. These profiles are similar at all energies, in particular at high energies where the component separation is more reliable thanks to the better angular resolution. The surface density of H\textsc{i} in the Perseus arm is on average 30\%–40\% higher than in the interarm region. Therefore, even if we adopt \(T_S = 400\) K which gives the largest arm–interarm contrast, the coupling scale (or the coupling length) between the CRs and matter (e.g., Hunter et al. 1997) required to agree with the LAT data would be larger than those usually assumed for this type of model (~2 kpc, see e.g., Digel et al. 2001, Figure 7). Whether the true emissivity profile exhibits a small contrast between the arms or smoothly declines with distance is beyond our measurement capability without further constraints on the H\textsc{i} column density derivation. New H\textsc{i} absorption measurements will allow us to investigate this issue with better accuracy.

4.3.2. Comparison with a Propagation Model: the CR Gradient Problem

To compare with the second quadrant results (Abdo et al. 2010a), we have integrated the emissivities above 200 MeV for \(T_S = 125\) K. We find values of \((0.817 \pm 0.016) \times 10^{-26}\) photons \(\text{s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1}\), \((0.705 \pm 0.018) \times 10^{-26}\) photons \(\text{s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1}\), and \((0.643 \pm 0.022) \times 10^{-26}\) photons \(\text{s}^{-1} \text{sr}^{-1} \text{H-atom}^{-1}\) for the Local arm, interarm, and Perseus arm regions, respectively. The nearer value is about 20\% lower than in the second quadrant (which, however, samples very nearby clouds in the Gould Belt) and the outer ones compare very well with the second quadrant measurement over the same Galactocentric distance range. Despite the uncertainties due to the optical-depth correction (that might have a different impact in the two quadrants), both LAT studies consistently point to a slowly decreasing emissivity profile beyond \(R = 10\) kpc.

Let us consider the predictions by a CR propagation model to see the impact of such a flat profile on the CR source distribution and propagation parameters. We adopted a GALPROP model, starting from the configuration used for the run 54_77Xvarh7S which we used to predict the IC contribution. The CR source distribution in this model is

\[
f(R) = \left(\frac{R}{R_\odot}\right)^{1.25} \exp\left(-3.56 \cdot \frac{R - R_\odot}{R_\odot}\right),
\]

where \(R_\odot = 8.5\) kpc is the distance of the Sun to the Galactic center. As shown in Figure 12, this function is intermediate between the distribution of supernova remnants (SNRs) obtained from the \(\Sigma-D\) relation (Case & Bhattacharya 1998) and that traced by pulsars (Lorimer 2004). The boundaries of the propagation region are chosen to be \(R_h = 30\) kpc (maximum Galactocentric radius) and \(z_h = 4\) kpc (maximum height from the Galactic plane), beyond which free escape is assumed. The spatial diffusion coefficient is assumed to be uniform across the Galaxy and is taken as \(D_{\text{lat}} = \beta D_0 (\rho/4GV)\), where \(\beta = v/c\) is the velocity of the particle relative to the speed of light and \(\rho\) is the rigidity. We adopted \(D_0 = 5.8 \times 10^{28}\) cm\(^2\) s\(^{-1}\) and \(\delta = 0.33\) (Kolmogorov spectrum). Reacceleration due to the interstellar magnetohydrodynamic turbulence, which is thought to reproduce the observed B/C ratio at low energy, assumes an Alfvén velocity \(v_A = 30\) km s\(^{-1}\). The CR source distribution and propagation model parameters have been used often in the literature (see e.g., Strong et al. 2004a). We note that the same CR source distribution and similar propagation parameters are adopted in the GALPROP run used by Abdo et al. (2010a).

The left panel of Figure 13 compares the calculated profile (solid line) with LAT constraints (bow-tie plot bracketing the profiles obtained for different \(T_S\); see the left panel of Figure 11). The model is normalized to the LAT measurement in the innermost region. Despite the large uncertainties, LAT data lead
to a significantly flatter profile than predicted by our model; the LAT results indicate to a factor of two larger emissivity (CR energy density) in the Perseus arm even if we assume \( T_S = 100 \text{ K} \). The higher \( T_S \) makes the discrepancy larger, hence the conclusion is robust. Not using the \( E(B - V)_{\text{res}} \) map in the analysis does not change the conclusion, since the emissivities in the interarm region and the Perseus arm are almost unaffected by its presence.

The discrepancy between the \( \gamma \)-ray emissivity gradient in the Galaxy and the distribution of putative CR sources has been known as the ”gradient problem” since the COS-B era (e.g., Bloemen 1989). It has led to a number of possible interpretations, including, for the specific case of the outer Galaxy, the possibility of a very steep gradient in \( X_{\text{CO}} \) beyond the solar circle (Strong et al. 2004b). The emissivities in the outer Galaxy were more difficult to determine in the COS-B/EGRET era due to lower statistics and higher backgrounds. Now, thanks to the high quality of the LAT data and the improved component separation technique applied to gas line data, we measure a flat \( \text{H} \text{I} \) emissivity gradient in the outer Galaxy together with a flat evolution of \( X_{\text{CO}} \) over several kpc, so the gradient problem requires another explanation.

The most straightforward possibility is a larger halo size \( z_h \), as discussed by, e.g., Stecker & Jones (1977), Bloemen (1989), and Strong & Moskalenko (1998). We therefore tried several choices of \( z_h \) and \( D_0 \) as summarized in the dotted lines in the same figure. The values of \( D_0 \) are chosen to reasonably reproduce the LIS of protons and electrons, \( B/C \) ratio and \( ^{10}\text{Be}/^{9}\text{Be} \) ratio at the solar system, and are similar to those given in Strong & Moskalenko (1998). All models are normalized to the LAT data in the Local arm. Models with \( z_h = 4 \text{ kpc} \) or smaller are found to give too steep emissivity gradients. A CR source distribution as in Equation (2) with a very large halo \( z_h \) provides a gradient compatible with the \( \gamma \)-ray data, if we fully take into account the systematic uncertainties.

We note that \( z_h = 10 \text{ kpc} \) is still compatible with \( ^{10}\text{Be}/^{9}\text{Be} \) measurements (e.g., Strong & Moskalenko 1998).

Considering the large statistical and systematic uncertainties in the SNR distribution, a flatter CR source distribution in the outer Galaxy also could be possible. We thus tried a modified CR source distribution, in which the distribution is the same as Equation (2) below \( R_{\text{bk}} \) and constant beyond it (see a thin solid line of Figure 12 as an example). Figure 13 right shows the models with several choices of \( R_{\text{bk}} \) for \( z_h = 4 \text{ kpc} \) and \( D_0 = 5.8 \times 10^{28} \text{ cm}^2 \text{ s}^{-1} \). We obtained a reasonable fit to the data using a flat CR source distribution beyond \( R = 10 \text{ kpc} \). Such a constant CR source density in the outer Galaxy is in contrast not only with the (highly uncertain) distribution of SNRs, but also with other tracers of massive star formation and SNRs, like, (1) \( \text{CO} \) lines which trace the interstellar phase where massive stars form (e.g., Ferri`ere 2001), (2) OB star counts (e.g., Bronfman et al. 2000), and (3) the \( ^{26}\text{Al} \) line which is related to the injection of stellar nucleosynthesis products in the ISM by SNRs (Diehl et al. 2006). However, a very large halo size and/or a flat CR source distribution just beyond the solar circle seem to be favored by the LAT data.

The above discussion depends on the propagation parameters and the solution is not unique. The exploration could be extended to other regions of the parameter space or to a non-uniform diffusion coefficient (e.g., Evoli et al. 2008), but examining propagation models in detail is beyond the scope of our study. Our bottom line is that the analysis of LAT data presented here and by Abdo et al. (2010a) consistently show that the CR density gradient in the outer Galaxy is flatter than expectations by commonly used propagation models. In the future, the extension to the inner part and the accurate determination of the gradient over the whole Galaxy will be key to constraining the CR origin and transport.

We also note that a spin temperature \( T_S \geq 250 \text{ K} \), which is favored by recent studies in the outer Galaxy (e.g., Dickey et al. 2009), gives a small arm/interarm contrast at the 10%–20% level that is not fully compatible with the propagation models (including the one we adopted here) which predict a monotonic CR gradient.

Even though the present analysis includes a dust template to account for the abundant missing gas present locally at the interface between the \( \text{H} \text{I} \) and CO-bright phases, an alternative way to reconcile the flat emissivity profile and a marked decline in CR density in the outer Galaxy is to invoke an increase in missing gas mass with Galactocentric distance in the low metallicity environments of the outer Galaxy (see, e.g., Papadopoulos et al. 2002; Wolfire et al. 2010) beyond the local correction applied here. We note that the large masses of dark gas in the outer Galaxy suggested by Papadopoulos et al. (2002)
We have studied the diffuse $\gamma$-ray emission in the third Galactic quadrant using the first 18 months of $\textit{Fermi}$ LAT science data. Thanks to the excellent performance of the LAT, we have obtained high-quality emissivity spectra of the atomic and molecular gas (traced by $W_{\text{CO}}$) in the 100 MeV–25.6 GeV energy range.

At the level of accuracy allowed by the LAT, the study of CR densities from $\gamma$-ray observations is now mostly limited by the understanding of the ISM mass tracers, notably by the uncertainties in the derivation of atomic gas column densities from H$_1$ surveys and by the distribution of gas not accounted for by radio and microwave line surveys. In spite of those uncertainties, robust conclusions can be drawn concerning the ISMs and CRs.

The molecular mass calibration ratio of the Local arm is found to be $\sim 2 \times 10^{20} \, \text{cm}^{-2} \, (\text{K} \, \text{km} \, \text{s}^{-1})^{-1}$, significantly larger than that for the very local Gould-Belt clouds in the second Galactic quadrant reported by Abdo et al. (2010a). No significant differences of the ratio are found between the Local arm and the interarm regions.

No significant variations in the CR spectra are found across the outer Galaxy in the region studied, and no large contrast in emissivity is seen in the interarm region between the Local and Perseus arms (a contrast < 10%–20% is allowed by data). The measured gradient is much flatter than predictions by a widely used propagation model assuming that the CR source distribution largely peaks in the inner Galaxy. A larger halo size and/or a flatter CR source distribution beyond the solar circle than those usually assumed are required to reproduce the LAT data, while other scenarios such as a non-uniform diffusion coefficient or vast amounts of missing gas in the outer Galaxy are also possible. Reliable determinations of the amount of atomic hydrogen in the plane are key to better constraining the property of CRs in our Galaxy.

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